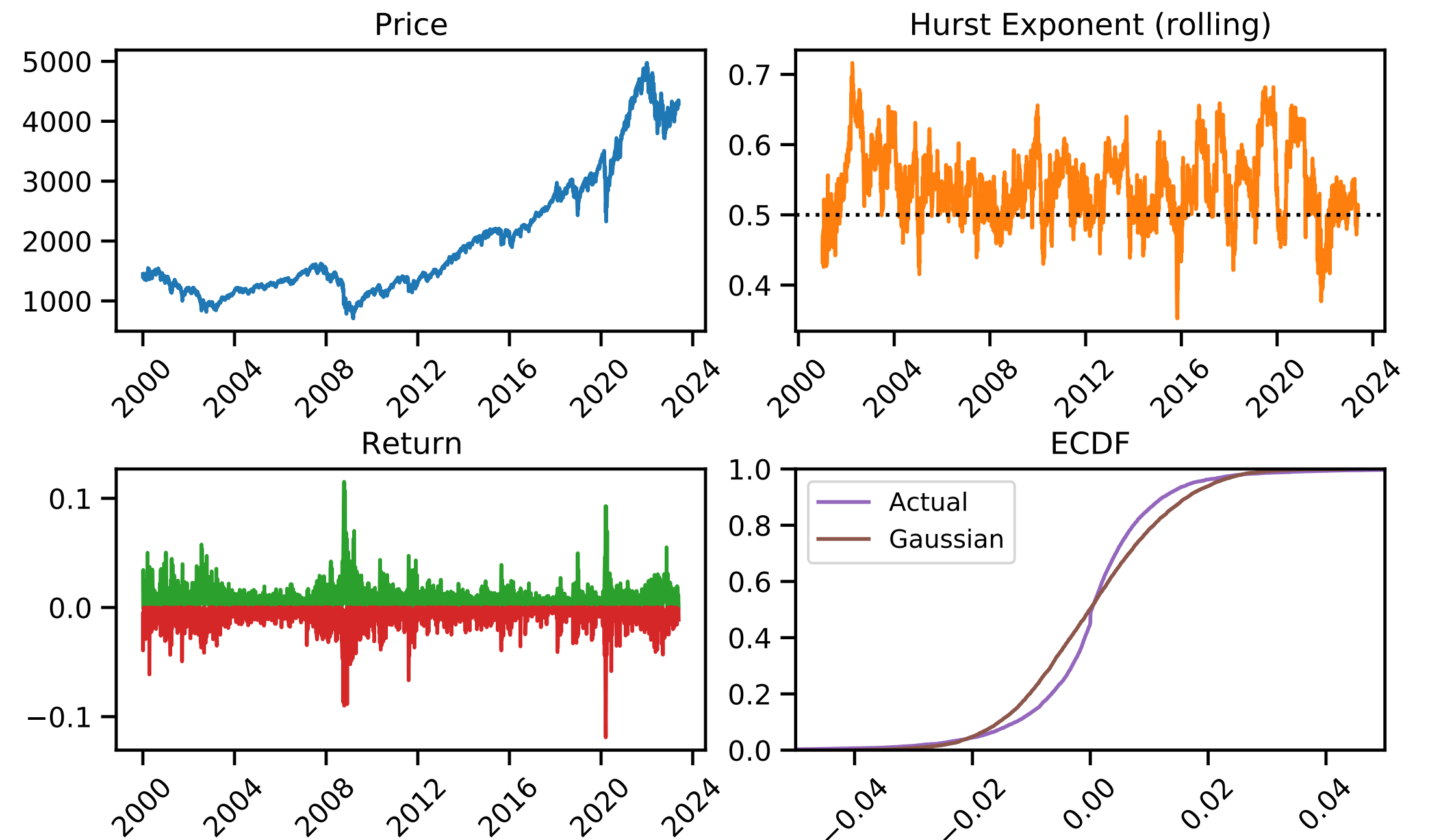


## Noise and Non-stationarity in Financial Machine Learning

**Financial Machine Learning** [2] differs from standard ML applications in many aspects, and in particular:

- Financial asset prices are **non-stationary** time-series, and differencing does not fully address the problem:
  - Asset returns are (negatively) autocorrelated and heteroscedastic, exhibiting volatility clusters
  - Their distribution is non-Gaussian, with large kurtosis ("fat-tails")
- Financial asset prices/returns exhibit a very poor signal-to-noise ratio, exposing ML models to overfitting.
  - E.g. Mean Hurst Exponent of daily S&P 500 closing price is around 0.54 (yearly lag).

### Example: S&P 500 Index



## Learning with Noisy Labels

Data come from a **noisy distribution**  $\tilde{\mathcal{D}} = \{(x_i, \tilde{y}_i)\}_{i=1}^N$ , with  $\tilde{\mathcal{Y}}$  being the noisy label space

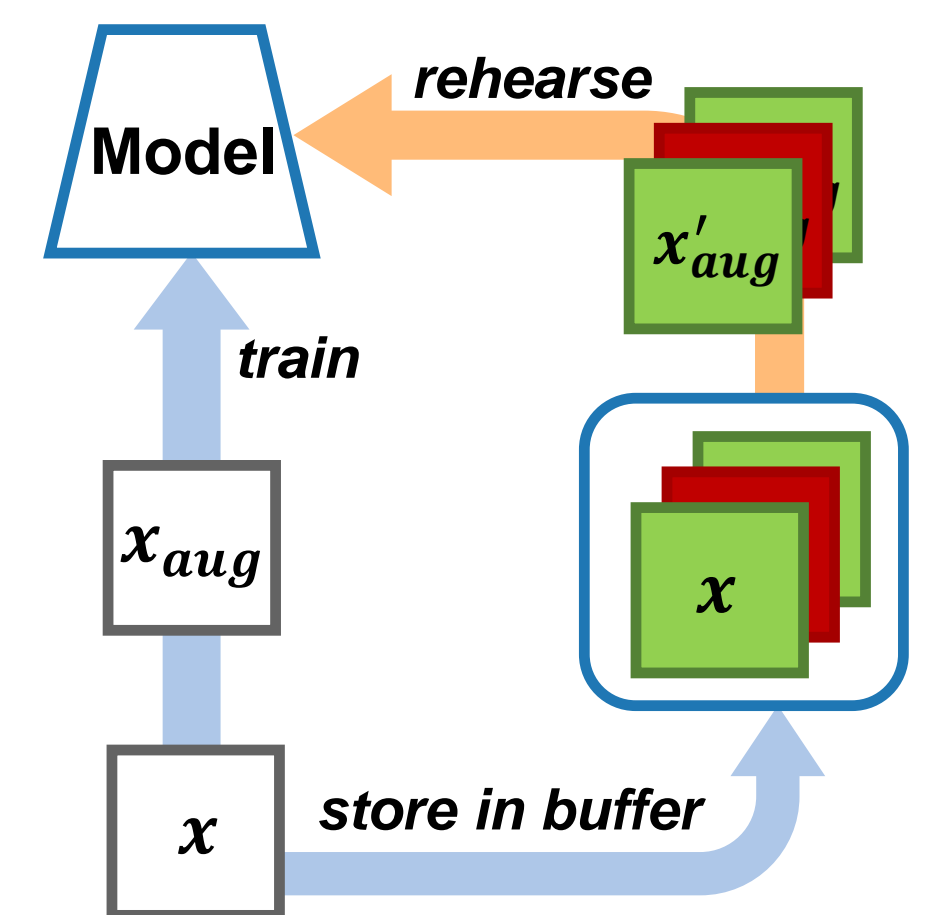


## Continual Learning

- Learning from a **sequence** of tasks  $\{\mathcal{D}_1, \dots, \mathcal{D}_T\}$
- Experience Replay (ER)**: train with current data stream  $\mathcal{D}_t$  and a buffer  $\mathcal{M}$  of past data

$$\theta^* = \arg \min_{\theta} \mathbb{E}_{(x, \tilde{y}) \sim \mathcal{D}_t} [\mathcal{L}(f(x), \tilde{y})] + \mathcal{L}_R$$

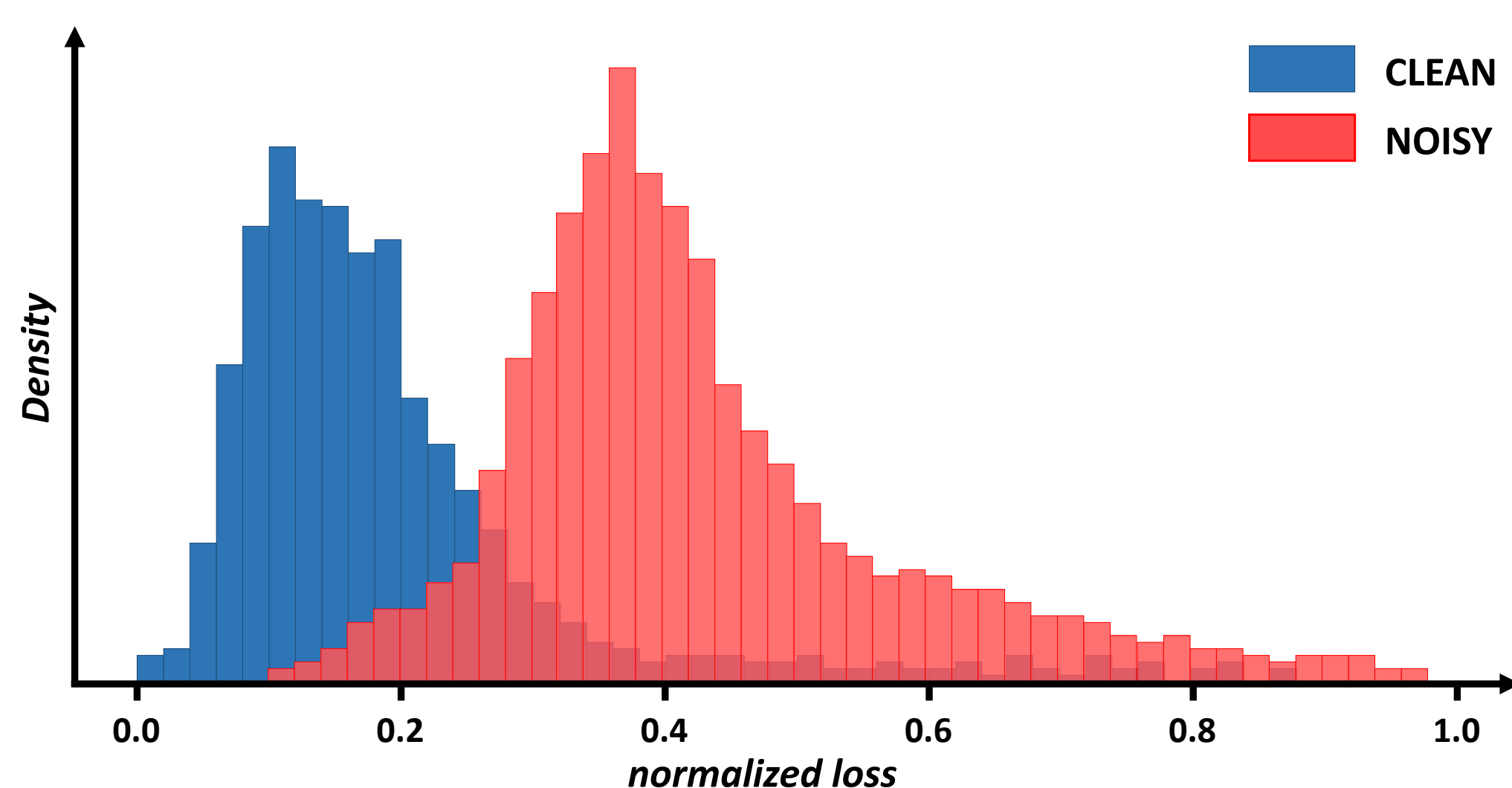
$$\mathcal{L}_R = \mathbb{E}_{(x_r, \tilde{y}_r) \sim \mathcal{M}} [\mathcal{L}(f(x_r), \tilde{y}_r)]$$



## Problem formulation and Experiments

**PROBLEM:** Samples from the noisy label space  $\tilde{\mathcal{Y}}$  are stored inside the buffer  $\mathcal{M}$

- Exploit **small-loss** criterion [3] to identify *clean* and *noisy* examples
- Fill the *replay memory*  $\mathcal{M}$  with the clean examples only, selected via Gaussian Mixture Model (GMM) or Oracle



Method	Split-N-CIFAR-10				
	Noise rate (symmetric)	0%	20%	40%	60%
Multitask		91.69	82.02	72.04	54.83
Finetuning		19.66	18.83	18.02	15.99
ER-ACE [1]		71.15	53.82	37.43	22.87
ER-ACE w/ Oracle		-	51.10	39.06	23.57
ER-ACE w/ GMM (OURS)		-	52.90	37.95	24.93

**Table 1:** Final Average Accuracy [ $\uparrow$ ] of ER with Asymmetric Cross Entropy (ER-ACE) combined with two different techniques to identify noisy samples and prevent storing them inside the memory buffer; comparison with some baseline methods.

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